

**From nuclear recoil track to MWPC signals
END-TO-END
DRIFT detector simulation**

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Presentation outline

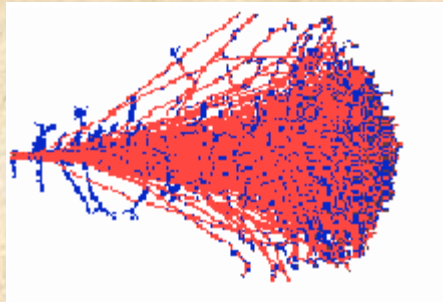
- Description of DRIFT END-TO-END simulation
 - Recoil track simulation using SRIM
 - Electric field and induced pulses simulation using GARFIELD
 - MWPC with repetitive readout response to a single positive ion moving from anode to grid wire/drift region
 - Read-out electronics: CREMAT amplifier and shaper
 - Signal shape sensitivity to:
 - diffusion
 - recoil direction
 - anode and grid signal simulation for X,Y,Z directed Sulfur recoils
-

END-TO-END Simulation

Steps of END-TO-END DRIFT detector simulation:

- Recoil track simulation with SRIM
 - reading file with 3D position of ionisation charge
 - 2. Electrons trap by CS₂ ions - NIP formation
(assumed 100% efficiency)
 - 3. Ionisation charge thermal diffusion in X,Y,Z
 $f=(\text{Electric field, Z position})$
 - 4. Electron detachment from NIP
(assumed 100% efficiency)
 - 4. Gas gain estimation for each NIP
 - 5. Charge induction calculation $f=(\text{time of positive ion motion in MWPC})$ for each NIP
 - 6. Transforming calculated charge into electric pulse
 - 7. Writing pulses into .ndd format file readable by DRIFT data analysis programs.
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The **S**topping and **R**ange of **I**ons in **M**atter : SRIM

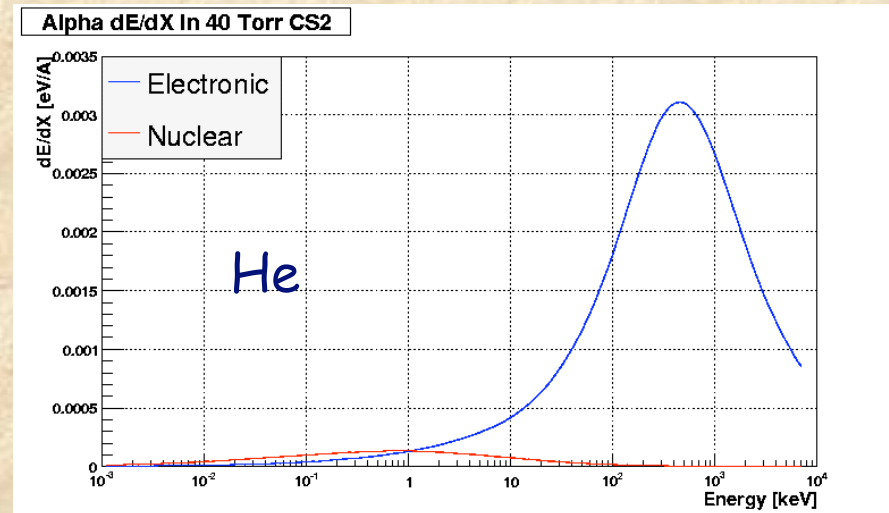
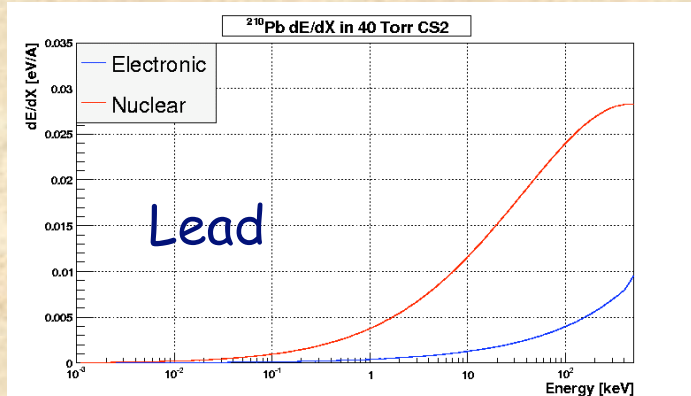
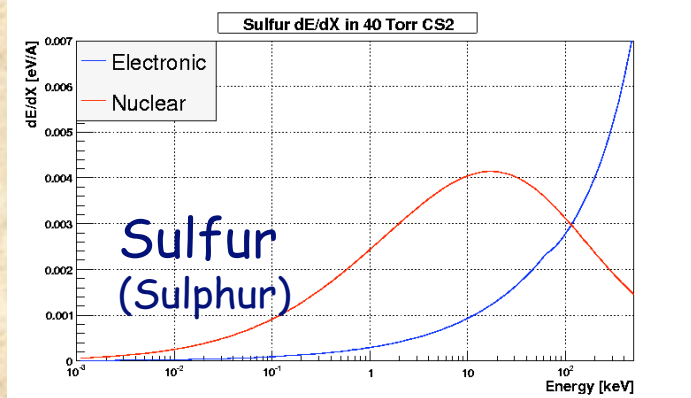
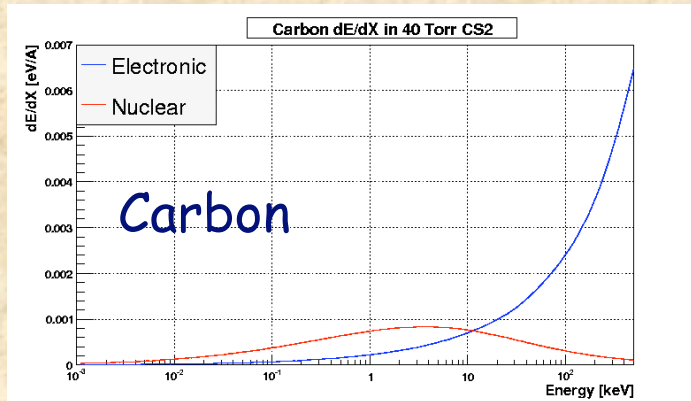


Simulation program developed by James F. Ziegler : calculates the stopping power and range of ions in matter.

SRIM includes TRIM (The **T**ransport of **I**ons in **M**atter) which calculates using MC a final 3D distribution of ions and cascading recoils created in the target.

Calculations of the stopping powers are based on the Brandt-Kitagawa theory (Phys. Rev. B25 (1982) 5631) which creates a formalism for scaling from proton stopping powers to that of any other ion at the same velocity .

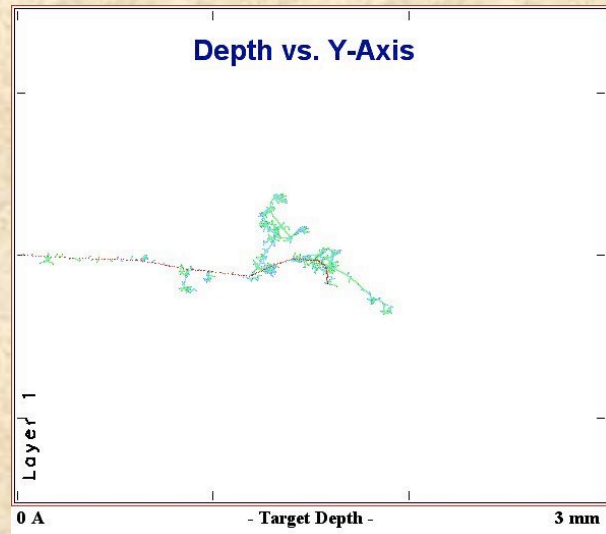
dE/dx for He, S, C and Pb in 40 Torr CS₂



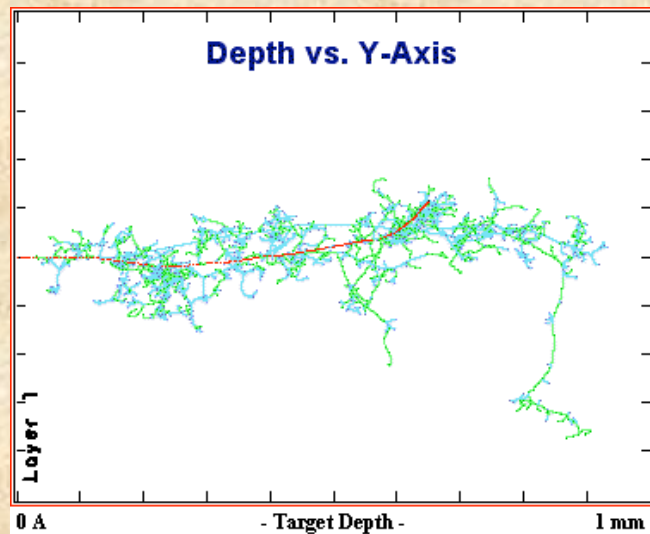
He loses energy mainly in electronic channel.

The heavier nuclear recoils the higher kinetic energy when energy loss in nuclear channel starts to dominate and the larger recoil cascade at the same ion energy.

Nuclear Recoil Cascades (SRIM)



Example of the nuclear recoil cascade from 100 keV S ion in 40 Torr CS2



Example of the nuclear recoil cascade from 103 keV Pb ion in 40 Torr CS2.

- red line : Pb ion
 - blue line : S recoils
 - green line : C recoils
-

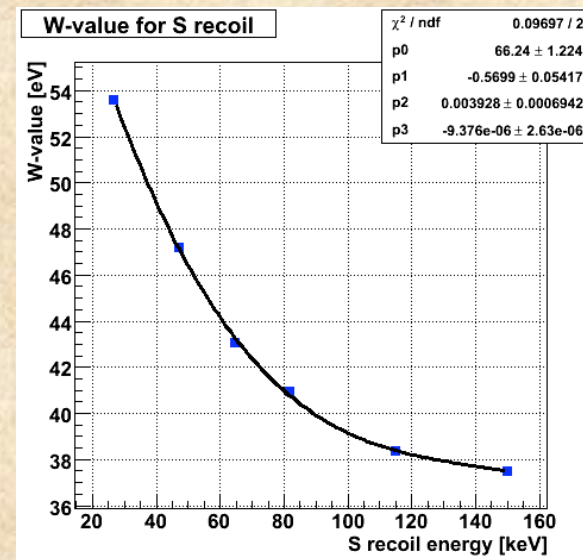
Nuclear recoil track: 3D ionisation charge distribution in space

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===== SRIM-2006.02 =====
=====
= Ion Energy vs Position File =
=====
= AXIS DEFINITIONS: X=Depth, Y,Z= Lateral plane of target surface.=
= (If beam enters target at an angle, this tilt is in Y direction)=
= Shown are: Ion Number, Energy (keV), X, Y, Z Position =
===== CALCULATION DATA =====
Ion Data: Name, Mass, Energy, Energy Interval
S 031.97 300keV 1eV
=====
Ion Number Energy (keV) Depth (X) (Angstrom) Y (Angstrom) Z (Angstrom) Energy Lost in Last Collision (eV)
-----
0000001 1.0000E+02 1.0000E+07 0.0000E+00 0.0000E+00 0.0000E+00
0000001 9.8871E+01 1.0220E+07 0.0000E+00 0.0000E+00 1.1291E+03
0000001 9.7841E+01 1.0440E+07 -5.8692E+03 4.1084E+03 1.0297E+03
0000001 9.7814E+01 1.0658E+07 -1.4129E+04 9.5749E+03 2.7161E+01
0000001 9.7809E+01 1.0876E+07 -2.3315E+04 1.8565E+04 4.8624E+00
0000001 9.7793E+01 1.1095E+07 -3.1891E+04 2.6139E+04 1.5695E+01
0000001 9.6649E+01 1.1313E+07 -3.8889E+04 3.1436E+04 1.1447E+03
0000001 9.6645E+01 1.1530E+07 -4.7882E+04 4.5119E+04 4.1359E+00
0000001 9.5787E+01 1.1747E+07 -5.6961E+04 5.9669E+04 8.5814E+02
0000001 9.4792E+01 1.1963E+07 -7.1806E+04 7.4139E+04 9.9462E+02
0000001 9.3883E+01 1.2178E+07 -8.6170E+04 8.9668E+04 9.0903E+02
0000001 9.3873E+01 1.2392E+07 -1.0420E+05 1.0765E+05 9.5665E+00
0000001 9.2830E+01 1.2605E+07 -1.2091E+05 1.2584E+05 1.0436E+03
0000001 9.1433E+01 1.2817E+07 -1.4161E+05 1.4836E+05 1.3964E+03
0000001 9.1423E+01 1.3024E+07 -1.8808E+05 1.7046E+05 1.0773E+01
0000001 9.0264E+01 1.3231E+07 -2.3675E+05 1.9302E+05 1.1586E+03
0000001 8.9239E+01 1.3440E+07 -2.6593E+05 2.0201E+05 1.0247E+03
0000001 8.8108E+01 1.3649E+07 -2.9530E+05 2.1495E+05 1.1312E+03
0000001 8.7175E+01 1.3857E+07 -3.1836E+05 2.3577E+05 9.3278E+02
0000001 8.6255E+01 1.4064E+07 -3.4046E+05 2.5527E+05 9.2063E+02
0000001 8.5328E+01 1.4271E+07 -3.6186E+05 2.7279E+05 9.2692E+02
0000001 8.4422E+01 1.4475E+07 -3.7349E+05 3.0946E+05 9.0536E+02
0000001 8.3522E+01 1.4678E+07 -3.8712E+05 3.4600E+05 9.0022E+02
0000001 8.2634E+01 1.4880E+07 -4.0114E+05 3.8374E+05 8.8816E+02
0000001 8.2387E+01 1.5082E+07 -4.1568E+05 4.2041E+05 2.4721E+02
0000001 8.1493E+01 1.5283E+07 -4.1898E+05 4.5744E+05 8.9389E+02
0000001 8.0760E+01 1.5485E+07 -4.2012E+05 4.9184E+05 7.3328E+02

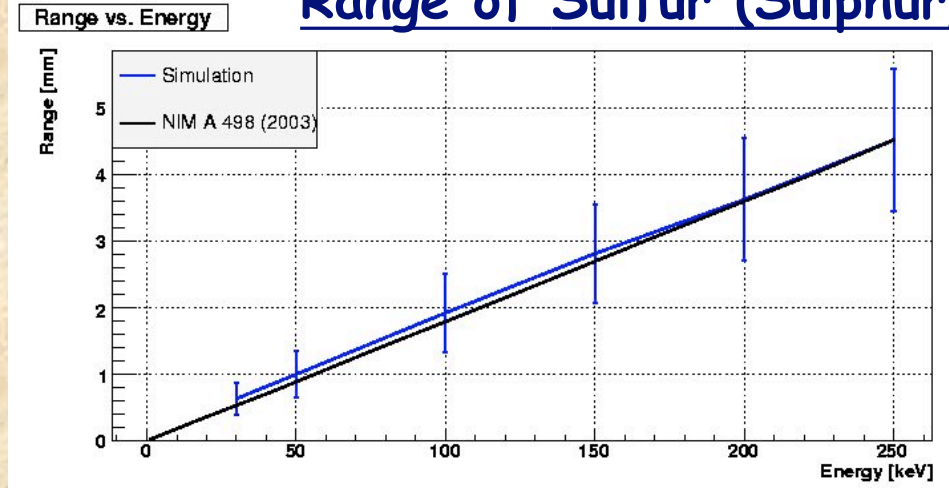
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Example of SRIM output:
- "EXYZ" file with: x, y, z
position of ion collisions and
energy lost
Number of ionisation charge
derivation from W-values :
 (Taken from NIMA 498 (2003) 155-164)



Nuclear recoil projected ranges

Range of Sulfur (Sulphur) recoils

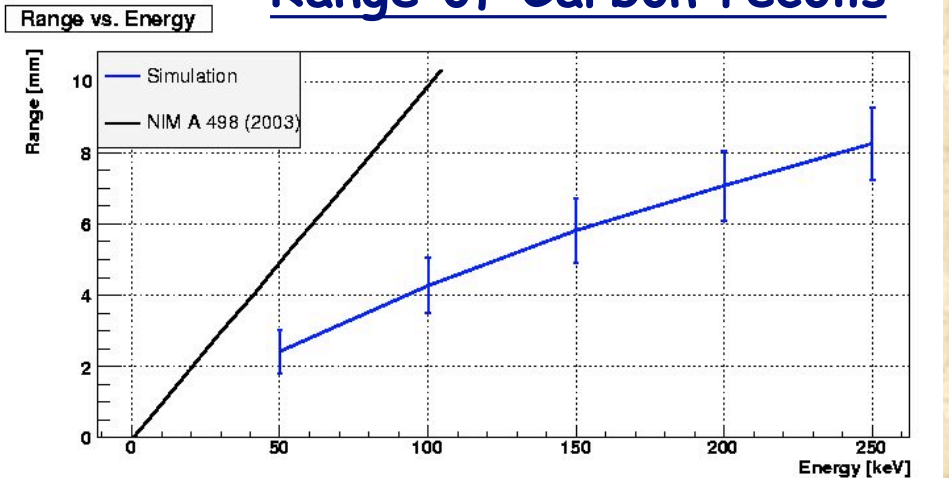


SRIM simulation results comparison with measurements:

-Very good agreement for Sulfur (Sulphur) recoils

-Large difference for Carbon recoils

Range of Carbon recoils



Simulation error bar - 1σ

Thermal Ion Diffusion

Diffusion suppressed to thermal level:

$$\sigma = \sqrt{\frac{4\epsilon_k L}{3eE}}$$

and

$$\epsilon_k = \frac{3}{2}k_B T$$


Hence:

$$\sigma [m] = \sqrt{\frac{L}{E}} \sqrt{\frac{2k_B T}{e}} \rightarrow \sigma [mm] = 0.72 \sqrt{\frac{L [m]}{E [\frac{kV}{cm}]}}$$

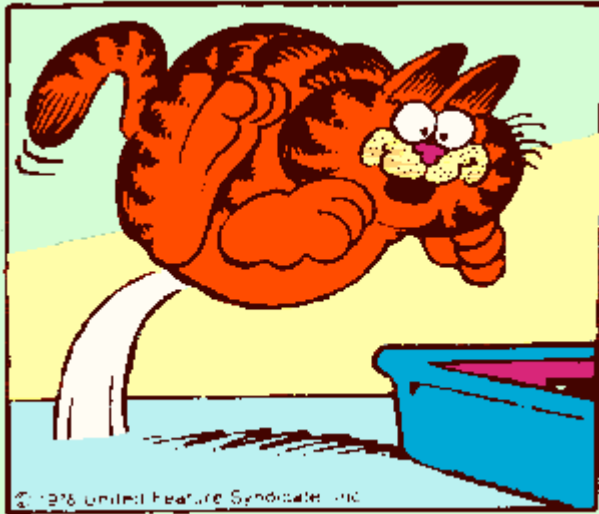
NIP drift distance



**Electric field in
detector drift
volume**



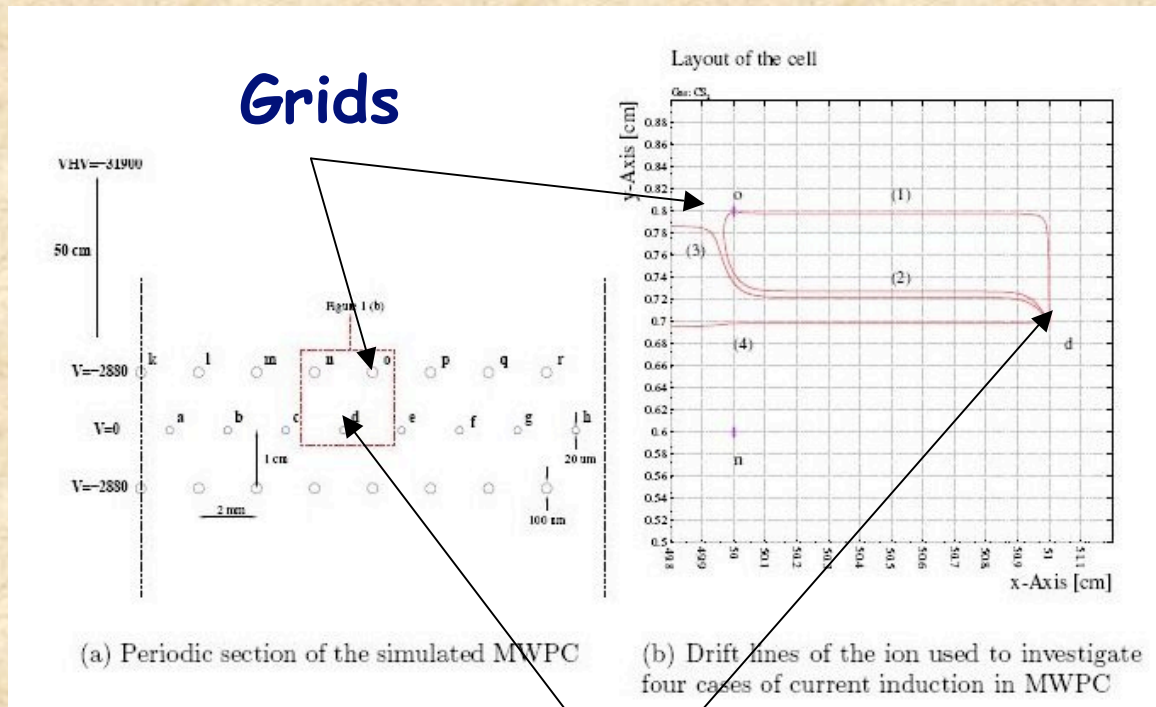
Electric field and induced currents calculation using Garfield



Garfield (written by R.Veenhof from CERN) :

- calculates 2D electric fields with wires and planes
 - accepts 2D and 3D external field Maps computed i.e by Maxwell, Tosca, FEMLAB ..
 - is interfaced to Magboltz and HEED programs for computation of charge transport in gases
 - calculates (with great precision) induced currents/charges on arbitrary electrode defined in the volume.
-

Signal induction in MWPC with crossed wires (2D approximation)



(a) Periodic section of the simulated MWPC

(b) Drift lines of the ion used to investigate four cases of current induction in MWPC

Calculation of currents induced on anode and grid in a periodic cell having 8 anode and 8 grid readout channels by avalanche ions moving along four representative drift lines (1-4)

Anodes

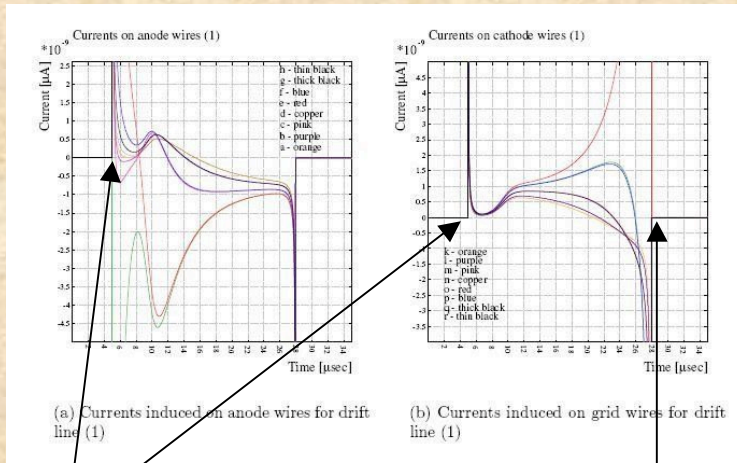
Lines (1-2) start from the anode and end on the grid

Lines (3-4) start from the anode and go into drift volume

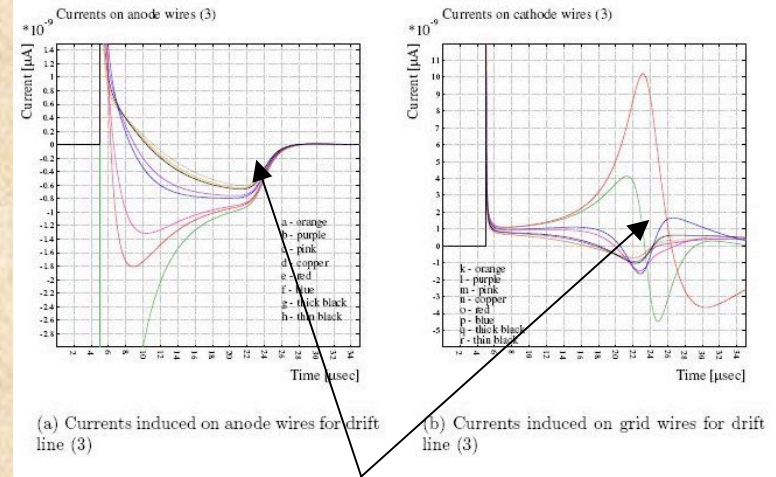
Induced currents

Anode/Grid currents (left/right plot)

Line 1



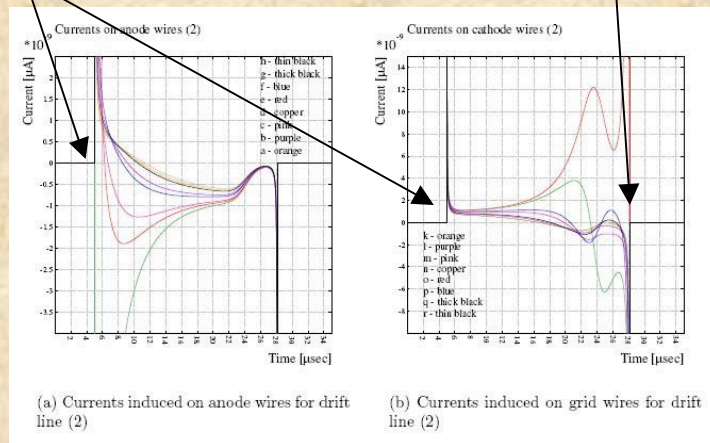
Line 3



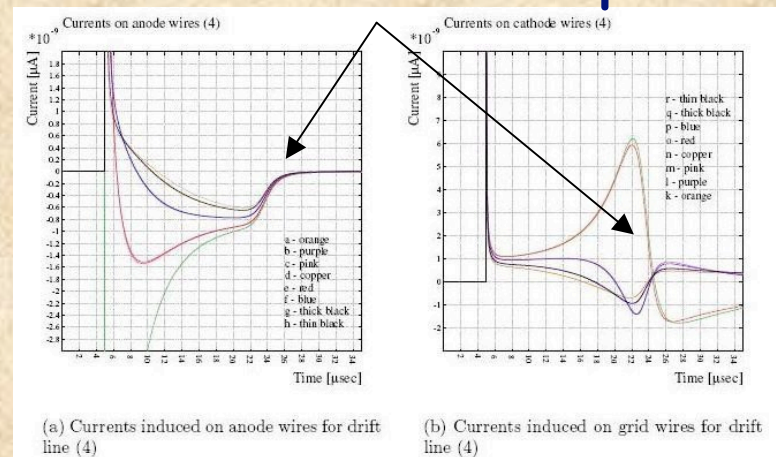
Ion starts drifting

Ion arrives to grid

Line 2



Line 4

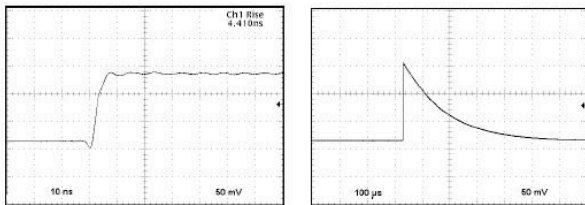


Ion passes grid wires, current without sharp end.

Positive ion drift velocity in MWPC $V=4 \cdot NIPs$ drift velocity ($E_{MWPC} \sim 4 \cdot E_{drift}$)

From induced charge to readout electric pulse

CREMAT CR-111 charge preamplifier output: 0.15 V/pC



cremat

Creemat, Inc.
45 Union St.
Watertown, MA 02472
(617) 527-6590
FAX: (617) 527-2849
<http://cremat.com>

Specifications

Assume temp = 20 °C, $V_s = \pm 6.1V$, unloaded output

	CR-111	units
Preamplification channels	1	
Equivalent noise charge (ENC)*	630	electrons
ENC RMS	0.1	femtoCoul.
Equivalent noise in silicon	6	keV (FWHM)
ENC slope	3.7	elect. RMS /pF
Gain	0.15	volts /pC

CREMAT CR-200 pulse shaper output: Gaussian pulse with shaping time $\sigma = 4 \mu s$ and fixed gain $\times 10$.

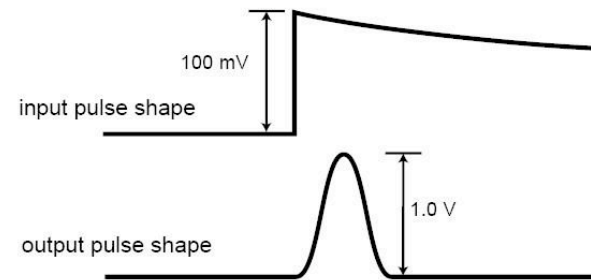


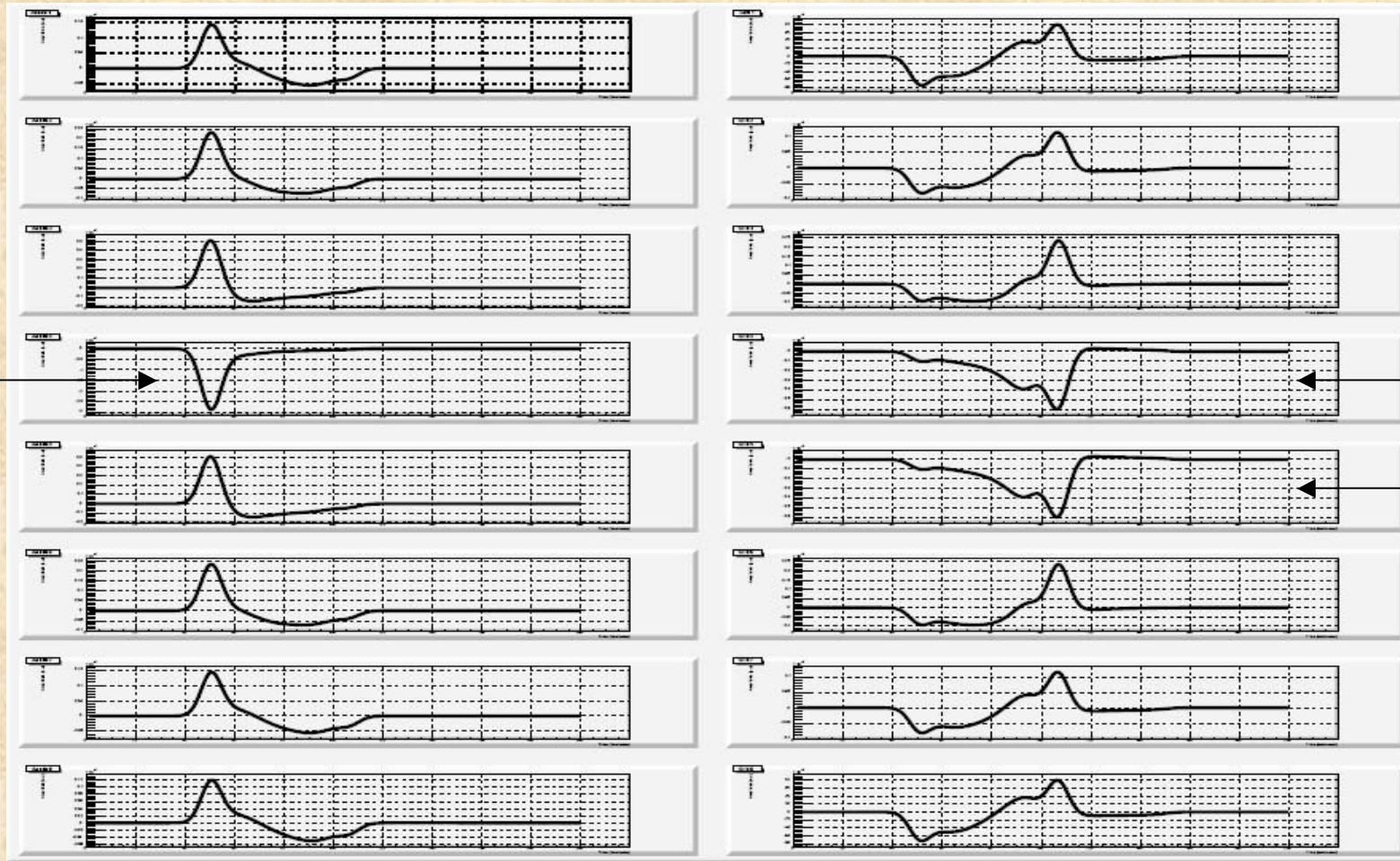
Figure 1. Comparison of sample input and output pulse shapes

Integration of induced currents- within each $1 \mu s$ window response from CR-111-CR-200 chain is calculated and summed over entire ion drift time giving total signal output from each anode and grid readout channel

Final signal look-up map

Anode pulses

Grid pulses

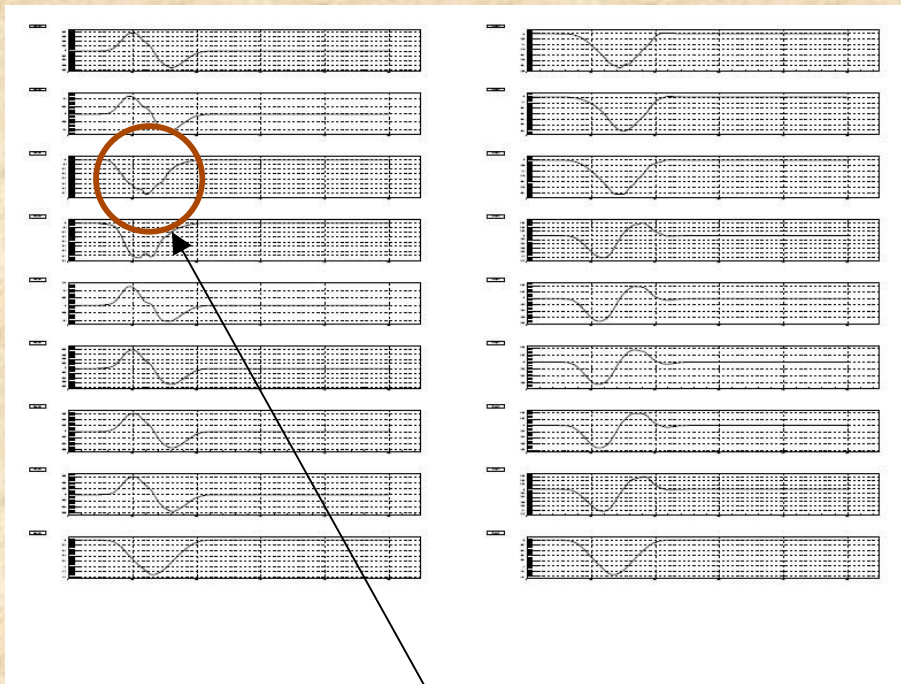


Anode (with avalanche) 1/6 scale

Grids on which avalanche ions landed
1/2 scale

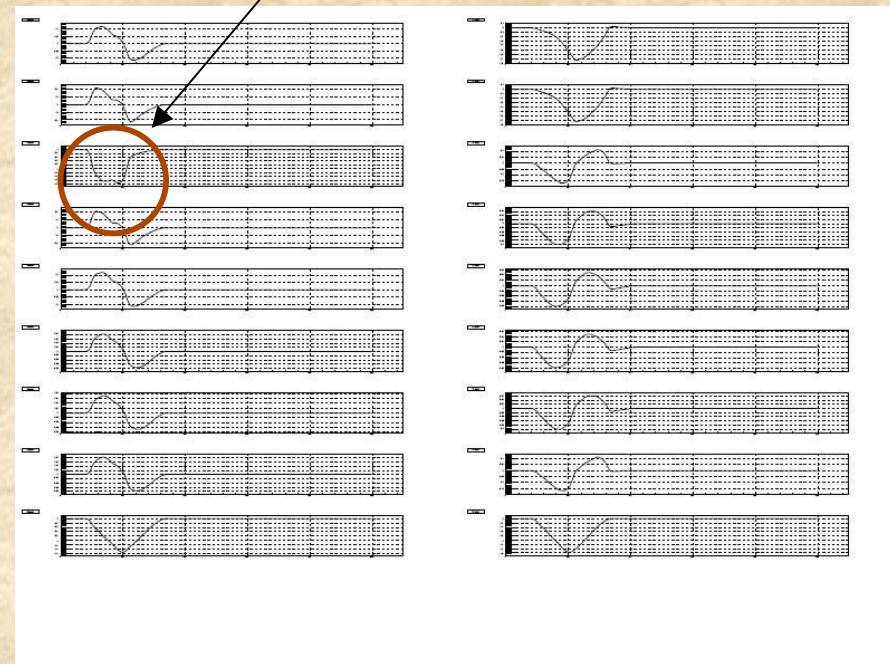
Final pulse from the track = SUM of pulses from all NIPs

Pulse shape from a track with and without diffusion

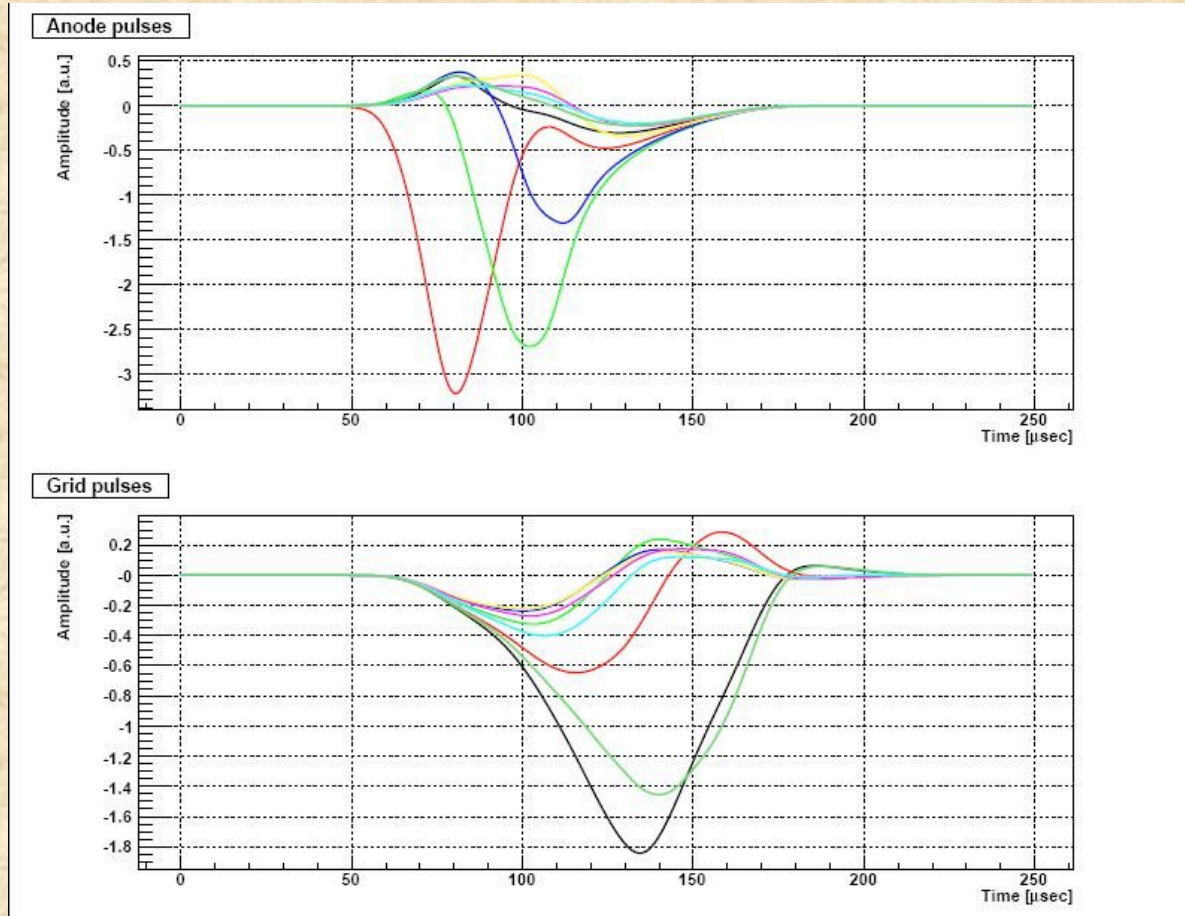


Diffusion over 50 cm
of drift

Zero diffusion



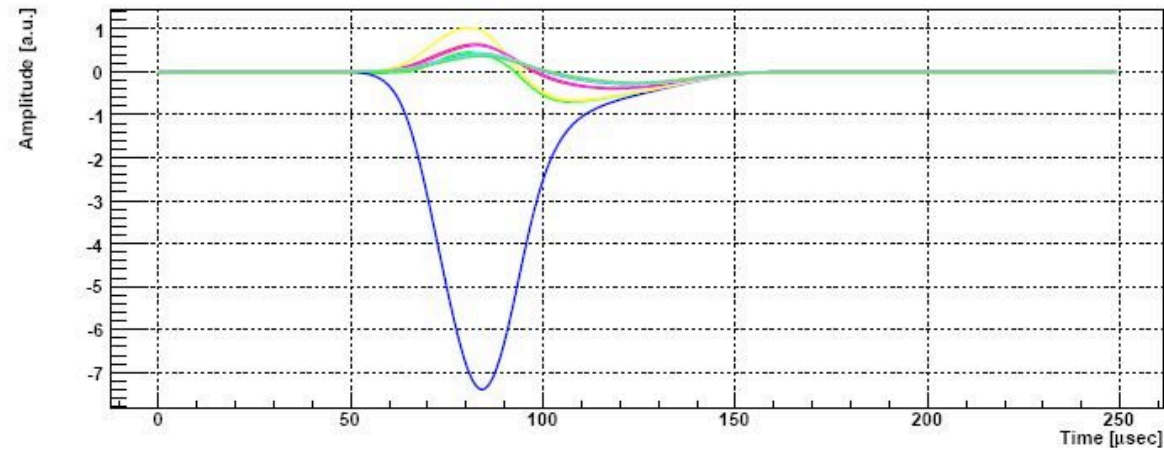
Directional 250 keV S recoils



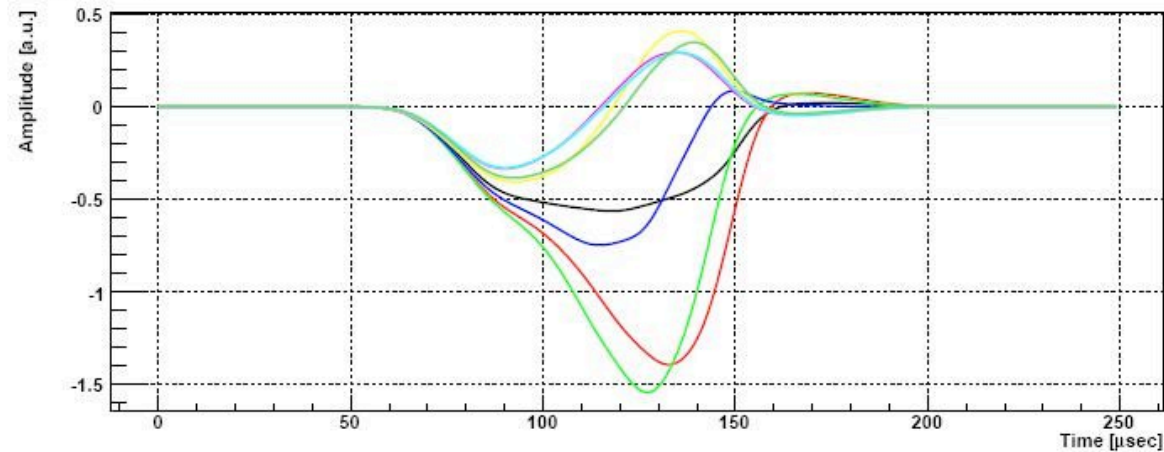
X-run:
Many anode
wires hit

Directional 250 keV S recoils

Anode pulses



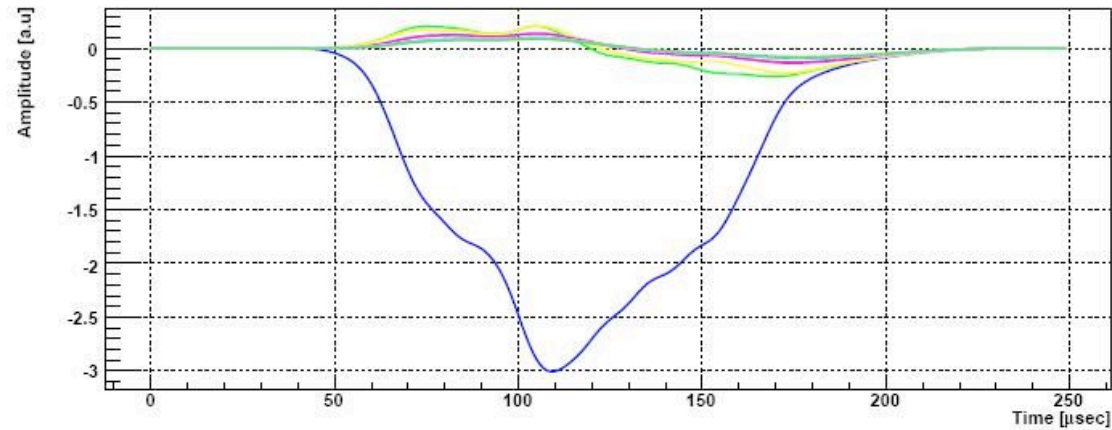
Grid pulses



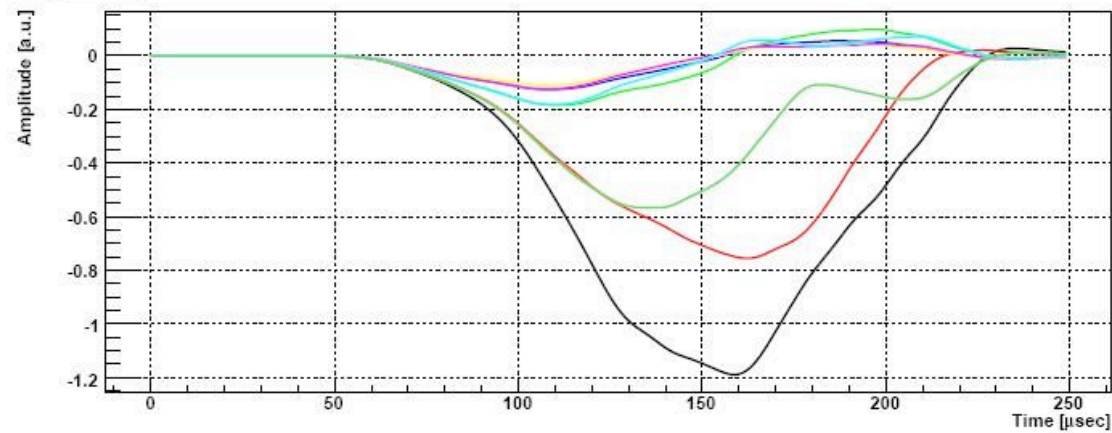
Y-run:
Many grid
wires hit

Directional 250 keV S recoils

Anode pulses



Grid pulses



Z-run:
Long pulses

Conclusions

DRIFT END-TO-END simulation program has been described. It is in its early stage and is under the process of validation.

Its validation with DRIFT data analysis program will be presented by Demitri Muna.

Thank you.
