Modern cosmology 4: The cosmic microwave background

- Expectations
- Experiments: from COBE to Planck
 - ► COBE
 - ▶ ground-based experiments
 - ► WMAP
 - ► Planck
- Analysis
- Results

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Analysis of WMAP data: the power spectrum

• Resolution and sky coverage

- beam profiles mapped by looking at Jupiter (a microwave source of known size)
 - sizes range from 49' to 13' depending on frequency
 - this corresponds to $\ell_{max} \sim 800$
- orbit around L2 covers whole sky every 6 months

WMAP beam profiles from L. Page et al, 2003, *ApJS*, **148**, 39



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Analysis of WMAP data: the power spectrum

• Instrumental noise

- WMAP has 10 radiometer assemblies (each with 2 receivers of different polarisation) covering 5 frequencies
 - derive angular power spectrum by cross-correlating measurements from maps by different radiometers
 - this cancels out noise properties of individual radiometers



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Results

• WMAP team extract parameters including

- ► baryon density $\Omega_{\rm b}h^2$
- matter density $\Omega_{\rm m}h^2$
- neutrino mass m_v
- ► Hubble constant *h*
- optical depth to reionisation τ



- ▶ spectral index of fluctuations *n*
- ▶ overall normalisation A

• to WMAP alone or WMAP with various other data

Combined Analyses

- What other data samples can be used?
 - ► WMAP 9-year analysis uses baryon acoustic oscillations (i.e. galaxy redshift surveys) and an independent measurement of H₀
 - power spectrum of luminous red galaxies can be used instead of standard galaxy survey data
 - ► H₀ = 73.8±2.4 km s⁻¹ Mpc⁻¹, Riess et al. (2011), from SNe Ia at z < 0.1</p>
 - WMAP 5-year analysis used baryon acoustic oscillations and Type Ia supernovae
 - WMAP9 restricts use of SNe Ia because of significant systematic errors

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Parameter	Planck	WMAP9	W9+BAO + <i>H</i> ₀
п	0.962 ± 0.009	0.972 ± 0.013	$\boldsymbol{0.971 \pm 0.010}$
τ	$\textbf{0.097} \pm \textbf{0.038}$	$\textbf{0.089} \pm \textbf{0.014}$	$\textbf{0.088} \pm \textbf{0.013}$
h	$\boldsymbol{0.674 \pm 0.014}$	0.700 ± 0.022	0.693 ± 0.009
$\Omega_{ m b}h^2$ %	2.207 ± 0.033	2.264 ± 0.050	2.266 ± 0.043
$\Omega_{ m cdm} h^2$ %	11.96 ± 0.31	11.38 ± 0.45	11.57 ± 0.23
Σm_{v}	<0.23 eV	<1.3 eV	<0.58 eV*
Ω_{k}	0.0000±0.00671	-0.037 ± 0.043	$-0.0027 \pm 0.0039*$
W	$-1.13^{+0.13}_{-0.10}$	$-1.1 \pm 0.4*$	$-1.07\pm0.09*$

Results from different data

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• = includes ground-based CMB data (SPT, ACT) ¹ = includes WMAP polarisation

Consistency checks

- Compare CMB results with other data
 - ► good consistency with galaxy redshift surveys
 - ► not such good consistency with H₀
 - Planck and, to lesser extent, WMAP9 prefer lower value
 - note that CMB estimates of *H*₀ are rather model dependent



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Conclusions

- Agreed features of best fit cosmological model
 - ▶ the universe is flat to high precision
 - ► as expected from inflation
 - ▶ no evidence of significant neutrino contribution
 - ▶ no hot dark matter
 - number of neutrinos consistent with 3
 - ▶ dark energy is consistent with cosmological constant

▶ w ≃ -1

 $\blacktriangleright \Omega_{\Lambda} \approx 0.7, \Omega_{\rm m0} \approx 0.3, H_0 \approx 70 \text{ km/s/Mpc}$

▶ but some disagreement about exact values

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Consequences

$$\dot{a}(t)^{2} = H_{0}^{2} \left(\frac{\Omega_{m0}}{a(t)} + (1 - \Omega_{m0}) a(t)^{2} \right)$$

- Universe is dominated by matter and Λ
- Universe is currently accelerating

$$\blacktriangleright \ddot{a}(t_0) = H_0^2 (1 - \frac{3}{2} \Omega_{\rm m0}) > 0$$

- ► acceleration started when $\Omega_{m0}/a^2 = 2(1 \Omega_{m0})a$, i.e. $a = 0.613 \pm 0.016$ or $z = 0.632 \pm 0.043$ (Planck) $a = 0.600 \pm 0.014$ or $z = 0.666 \pm 0.039$ (SFH13)
 - consistent with supernova results

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Consequences

$$\dot{a}(t)^{2} = H_{0}^{2} \left(\frac{\Omega_{m0}}{a(t)} + (1 - \Omega_{m0}) a(t)^{2} \right)$$

can be integrated (slightly messily) to give

$$H_0 t = \frac{2}{3\sqrt{1 - \Omega_{m0}}} \sinh^{-1} \left(\sqrt{\frac{1 - \Omega_{m0}}{\Omega_{m0}}} a^{3/2} \right)$$

which enables us to calculate the age of the universe, proper distances, expansion as a function of time, etc.

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Conclusions

- Data from the HST, supernovae, galaxy surveys and the CMB have enabled us to determine cosmological parameters to within a few percent
 - ► different sources are basically consistent—need to wait and see if low Planck H₀ significant
- Data now provide strong constraints on theories

▶ "benchmark" ACDM hard to beat

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Where are we?

- We have a first class description of the Universe
 - ▶ its content, its age, its likely future
- We do not have good explanations for some aspects
 - ▶ the nature of dark matter (can LHC help?)
 - ► (especially) the nature of dark energy
 - ▶ the actual values of the parameters
- Immense progress in the last 15 years, but much still to do!

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